



# Beijing-Dublin International College



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## SEMESTER 2 EXAMINATION - 2018/2019

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School of Computer Science

### COMP2003J Data Structures and Algorithms 2

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Dr. Rosemary Monahan  
Dr. David Lillis  
Dr. Takfarinas Saber\*

**Time Allowed: 120 minutes**

### Instructions for Candidates

Answer any 2 questions. All questions carry equal marks.

**BJUT Student ID:** \_\_\_\_\_ **UCD Student ID:** \_\_\_\_\_

I have read and clearly understand the Examination Rules of both Beijing University of Technology and University College Dublin. I am aware of the Punishment for Violating the Rules of Beijing University of Technology and/or University College Dublin. I hereby promise to abide by the relevant rules and regulations by not giving or receiving any help during the exam. If caught violating the rules, I accept the punishment thereof.

**Honesty Pledge:** \_\_\_\_\_ **(Signature)**

### Instructions for Invigilators

No special instructions.

## Question 1:

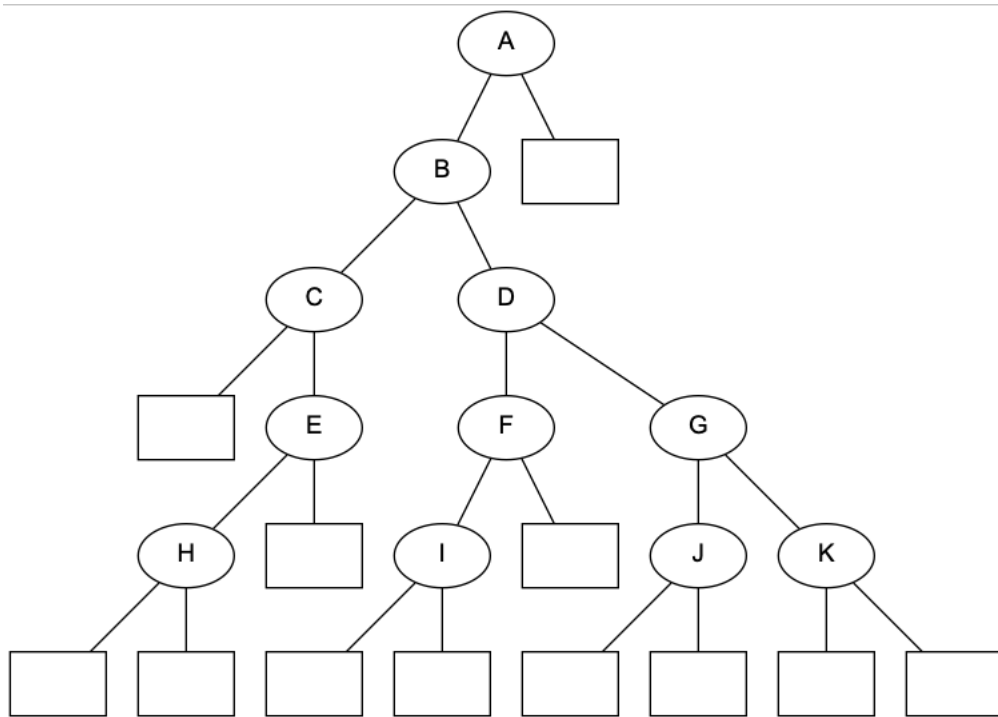


Figure 1

- (a) Study the tree in Figure 1 and answer the questions that follow.
- List the siblings of H.
  - What is the depth of E?
  - What is the degree of node F?
  - What is the height of the tree?
  - List the descendants of D.
  - Is (H,E) an edge? Explain your answer.
  - List the nodes that are in the subtree that is rooted at C.
  - Which of the following phrases is the best description for this tree: *binary search tree*, *proper binary tree*, *complete binary tree*. Explain your answer.

[8 marks]

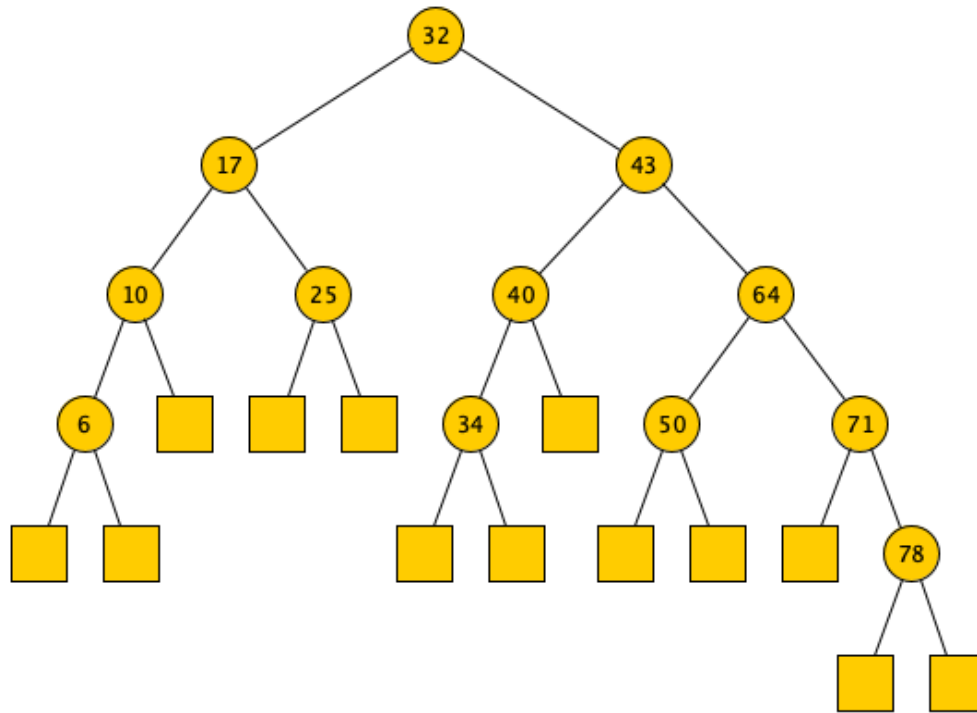


Figure 2

- (b) Assume that the tree in Figure 2 is an **AVL Tree**. Draw the state of the tree after performing the following operations. In your answer, you should show the tree's state after each step and mention any restructuring that is required.

- (i) Remove 25
- (ii) Insert 35
- (iii) Remove 50
- (iv) Insert 3
- (v) Remove 10

[12 marks]

- (c) With regard to analysing the performance of a **Binary Search Tree**, discuss each of the following:

- (i) Space requirements.
- (ii) Time complexity of the insert() and remove() functions.
- (iii) The effect that a balanced tree has on the time complexity has on the insert() and remove() functions.

[10 marks]

- (d) Assume that the tree in Figure 2 is a Splay Tree. If the next operation is to remove 78, draw trees to show all restructuring operations that will happen and state what restructuring operations these are.

[6 marks]

- (e) A Splay Tree is said to be balanced in the *amortised sense*. Briefly describe what is meant by this.

[4 marks]

- (f) Answer the following questions relating to the traversal of binary trees.

- (i) List the values found during a *postorder* traversal of the tree in Figure 2.
- (ii) List the values found during an *preorder* traversal of the tree in Figure 2.
- (iii) The following are two traversals of a binary tree. Draw the tree.

Preorder: H, C, A, F, D, E, B, G

Inorder: C, H, A, G, F, B, E, D

[10 marks]

[Total 50 marks]

**Question 2:**

- (a) Give definitions of the following graph concepts: *incident edges*, *adjacent vertices*, *degree of a vertex*, *paths*, and *cycles*.

[10 marks]

- (b) One implementation of a *priority queue* ADT is to use a *heap*.

- (i) Heaps make use of two key properties: the *order property* and the *structural completeness property*. Give definitions for each of these properties.

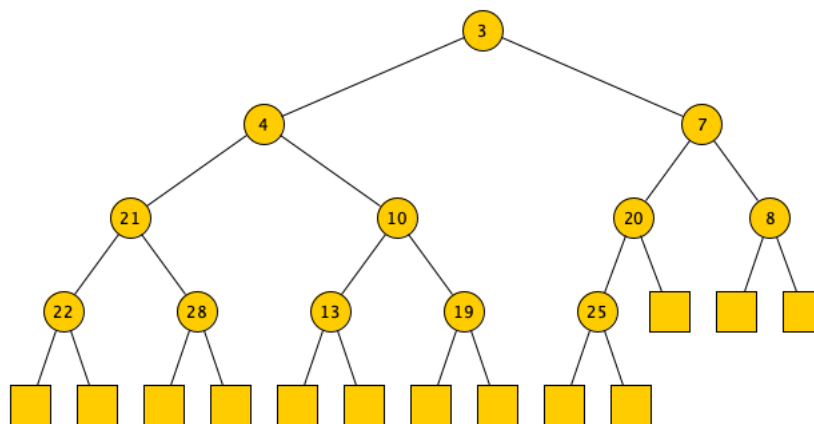
[4 marks]

- (ii) Describe the steps by which items are removed from a heap. Illustrate your answer by removing an item from the heap in Figure 3.

[6 marks]

- (iii) Describe the steps by which items are inserted into a heap. Illustrate your answer by inserting an item with priority 9 into the heap in Figure 3.

[6 marks]

**Figure 3**

- (c) An array-based list is an appropriate way to implement a *Complete Binary Tree*.

- (i) Explain in detail the advantages of using this type of implementation type compared to using a linked structure.

[6 marks]

- (ii) Why is an array-based list not suitable to represent an AVL tree?

[4 marks]

- (d) *Huffman Encoding* is a technique for text compression that uses a *Huffman Tree*. Using the string “go go gophers” as an example, describe in detail how a Huffman Tree is created and how it can be used to generate a code to represent the string.

[14 marks]

[Total 50 marks]

## Question 3:

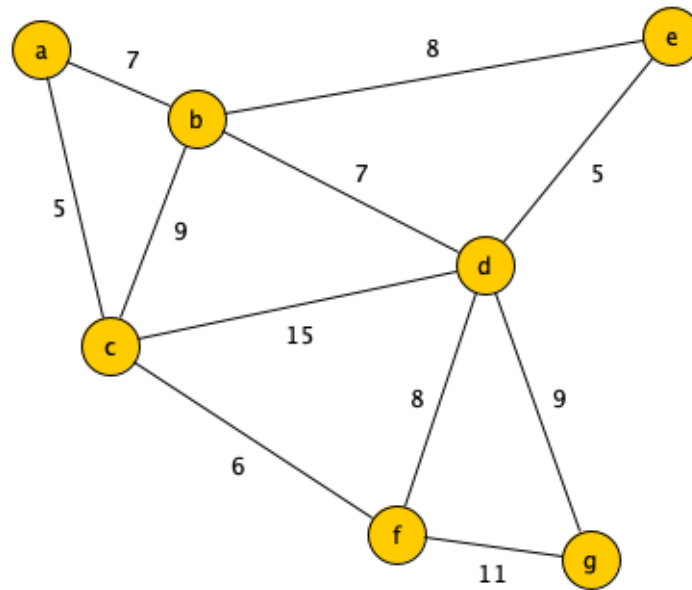


Figure 4

- (a) Using the graph in Figure 4 as an example, show how Kruskal's algorithm can be used to compute a *Minimum Spanning Tree*. In your answer, you must explain each step that you take.

[12 marks]

- (b) Using the graph in Figure 4 as an example, show how Dijkstra's algorithm can be used to compute a *shortest distance tree* beginning at the vertex containing "g". In your answer, you must explain each step that you take.

[12 marks]

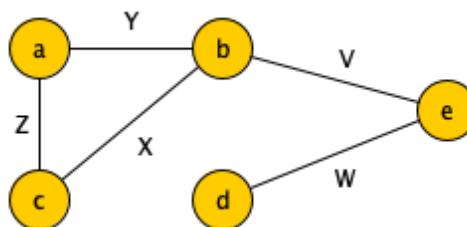


Figure 5

- (c) Draw a diagram to show how the graph in Figure 5 can be represented using an *adjacency matrix* structure. In your answer, describe each object type and data structure used to explain its purpose and what data it stores.

[12 marks]

- (d) There are three main implementation strategies for the Graph ADT: *edge list*, *adjacency list*, and *adjacency matrix*. Compare the performance of each implementation strategy for each of the following headings. In each case, briefly explain the reason for any difference in performance.
- (i) Space (memory) usage.
  - (ii) `incidentEdges(v)` method.
  - (iii) `areAdjacent(v,w)` method.
  - (iv) `removeVertex(v)` method.
  - (v) `removeEdge(e)` method.

[14 marks]

[Total 50 marks]